

# More Mathematics in Python

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## Built-In Functions/Constants

1. Calculate the absolute value of 7, and -7.
2. Determine the minimum value from the list: 4 -2 7 0 -1.
3. Determine the maximum value from the list: 18 3 -1 21 17.
4. Round  $\pi$  to 5 decimal places.
5. Round  $e$  to the nearest hundredth.

## Math Module

6. Calculate the square root of 20.
7. Calculate the distance,  $d$ , between the the points (7,5) and (3,-1), using the formula  $d = \sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$ .
8. Calculate  $\sin(2)$ , where 2 is in radians.
9. Convert  $60^\circ$  to radians.
10. Show that  $\cos(60^\circ)$  is  $\frac{1}{2}$ . Is the answer what you expected? Explain.
11. It is well known that  $\sin^{-1}(1) = 90^\circ$ , but the command `math.asin(1)` produces a value of 1.57. Why? Modify the command to produce a value of  $90^\circ$ .
12. In the non-right triangle  $ABC$ ,  $b=3$ ,  $c=5$  and  $A=35^\circ$ . Determine the length of side  $a$  using the formula  $a = \sqrt{b^2 + c^2 - 2bc \cdot \cos A}$ .
13. In the non-right triangle  $PQR$ ,  $p=6$ ,  $r=4$  and  $P=70^\circ$ . Determine the measure of angle  $R$  using the formula  $R = \sin^{-1}\left(\frac{r \sin P}{p}\right)$ .
14. Determine  $\log_{10}(1\ 000\ 000)$ .
15. Determine  $\log_2(512)$ .
16. Calculate the value of  $9!$
17. Determine the number of digits in the value of  $20!$
18. The number of ways to arrange  $n$  distinct objects in a line is given by  $n!$ . How many ways are there to arrange 12 distinct objects?
19. Determine  $\lfloor 5.8 \rfloor$  and  $\lfloor -5.8 \rfloor$ .
20. Determine  $\lceil 5.8 \rceil$  and  $\lceil -5.8 \rceil$ .
21. The number of *derangements* – ways in which  $n$  letters can be arranged, such that *none* of them appear in their alphabetical position – is given by  $d = \left\lfloor \frac{n!}{e} + \frac{1}{2} \right\rfloor$ . For example, there is one derangement of the letters A and B (B A) and two derangements of A B C (B C A and C A B). Use the formula to verify that the number of derangements for 1, 2, 3, 4 and 5 letters are 0, 1, 2, 9 and 44 respectively.